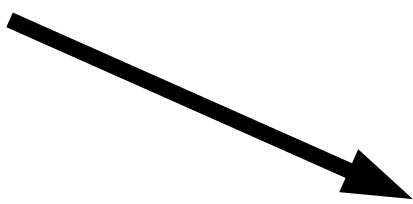


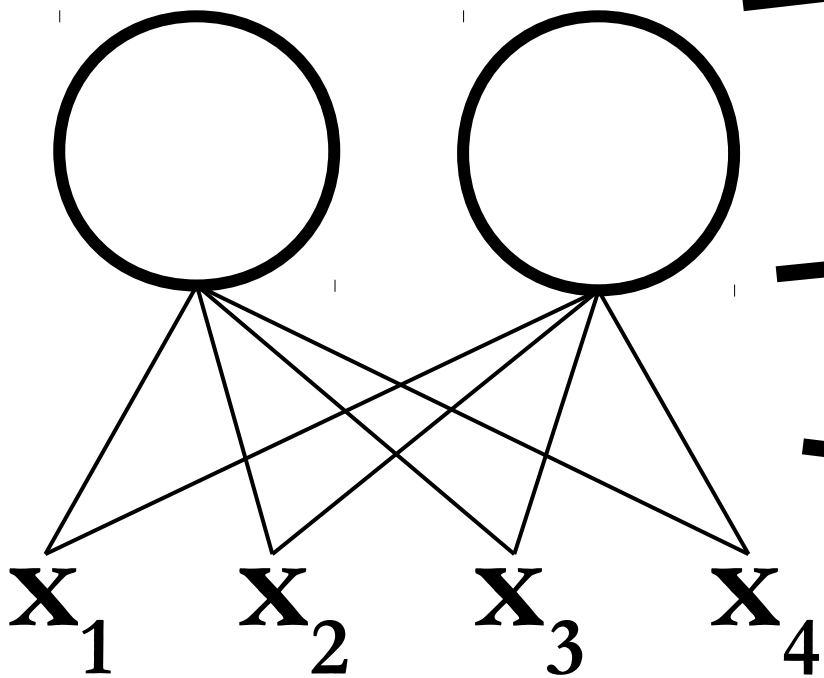
$$\begin{bmatrix} [1 & 0] \\ [1 & 1] \\ [0 & 1] \end{bmatrix}$$



$$\begin{bmatrix} [0.9 & 0.8 & -1.0 & -1.0] \\ [-0.5 & -0.5 & 1.5 & 1.0] \end{bmatrix}$$



$$\begin{bmatrix} [4.9 & 3.0 & 1.4 & 0.2] \\ [6.4 & 3.2 & 4.5 & 1.5] \\ [5.8 & 2.7 & 5.1 & 1.9] \end{bmatrix}^1$$



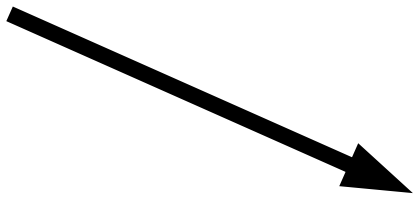
$$\begin{bmatrix} [1 & 0] \\ [1 & 1] \\ [0 & 1] \end{bmatrix}$$



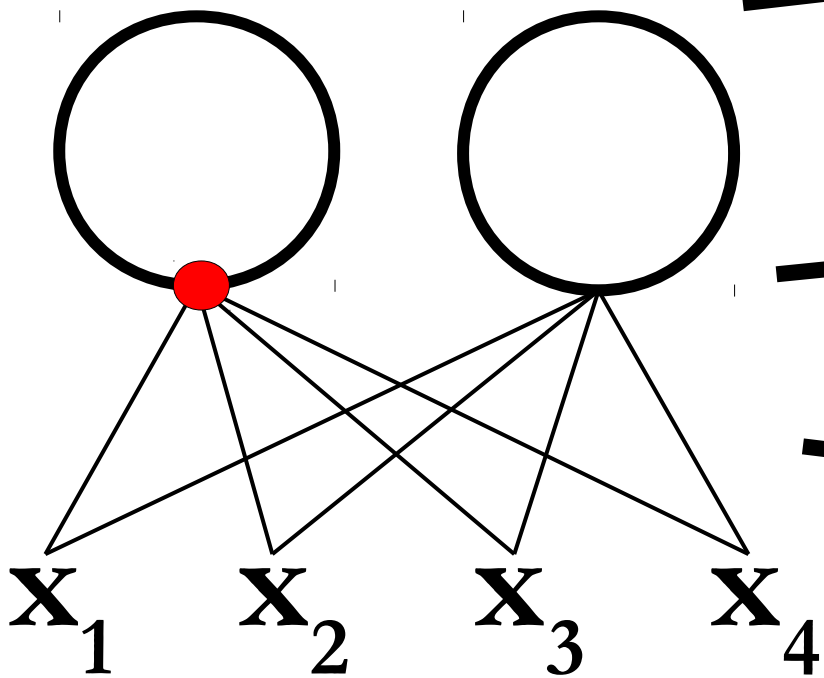
$$\begin{bmatrix} [5.21 & -1.65] \\ [2.32 & 3.45] \\ [0.38 & 5.30] \end{bmatrix}$$



$$\begin{bmatrix} [0.9 & 0.8 & -1.0 & -1.0] \\ [-0.5 & -0.5 & 1.5 & 1.0] \end{bmatrix}$$



$$\begin{bmatrix} [4.9 & 3.0 & 1.4 & 0.2] \\ [6.4 & 3.2 & 4.5 & 1.5] \\ [5.8 & 2.7 & 5.1 & 1.9] \end{bmatrix}^2$$

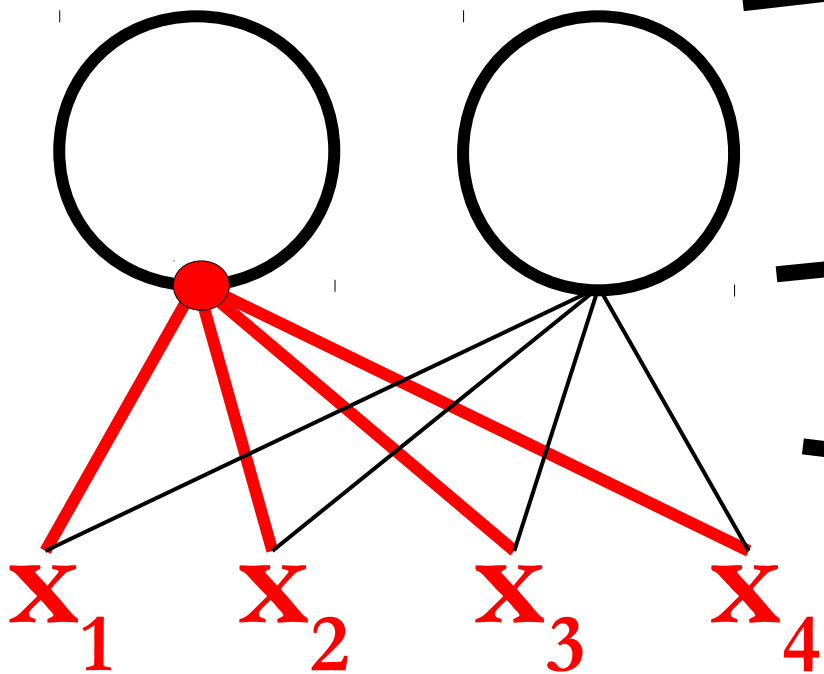


$\begin{bmatrix} 1 & 0 \\ 1 & 1 \\ 0 & 1 \end{bmatrix}$

$\begin{bmatrix} 5.21 & -1.65 \\ 2.32 & 3.45 \\ 0.38 & 5.30 \end{bmatrix}$

$\begin{bmatrix} 0.9 & 0.8 & -1.0 & -1.0 \\ -0.5 & -0.5 & 1.5 & 1.0 \end{bmatrix}$

$\begin{bmatrix} 4.9 & 3.0 & 1.4 & 0.2 \\ 6.4 & 3.2 & 4.5 & 1.5 \\ 5.8 & 2.7 & 5.1 & 1.9 \end{bmatrix}$ <sup>3</sup>

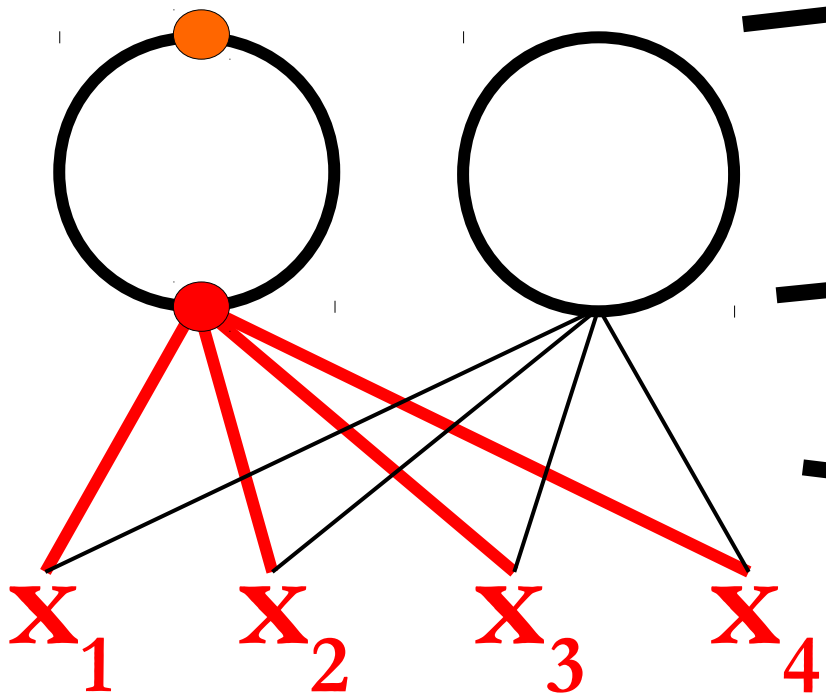


$$\begin{bmatrix} 1 & 0 \\ 1 & 1 \\ 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 5.21 & -1.65 \\ 2.32 & 3.45 \\ 0.38 & 5.30 \end{bmatrix}$$

$$\begin{bmatrix} 0.9 & 0.8 & -1.0 & -1.0 \\ -0.5 & -0.5 & 1.5 & 1.0 \end{bmatrix}$$

$$\begin{bmatrix} 4.9 & 3.0 & 1.4 & 0.2 \\ 6.4 & 3.2 & 4.5 & 1.5 \\ 5.8 & 2.7 & 5.1 & 1.9 \end{bmatrix}$$

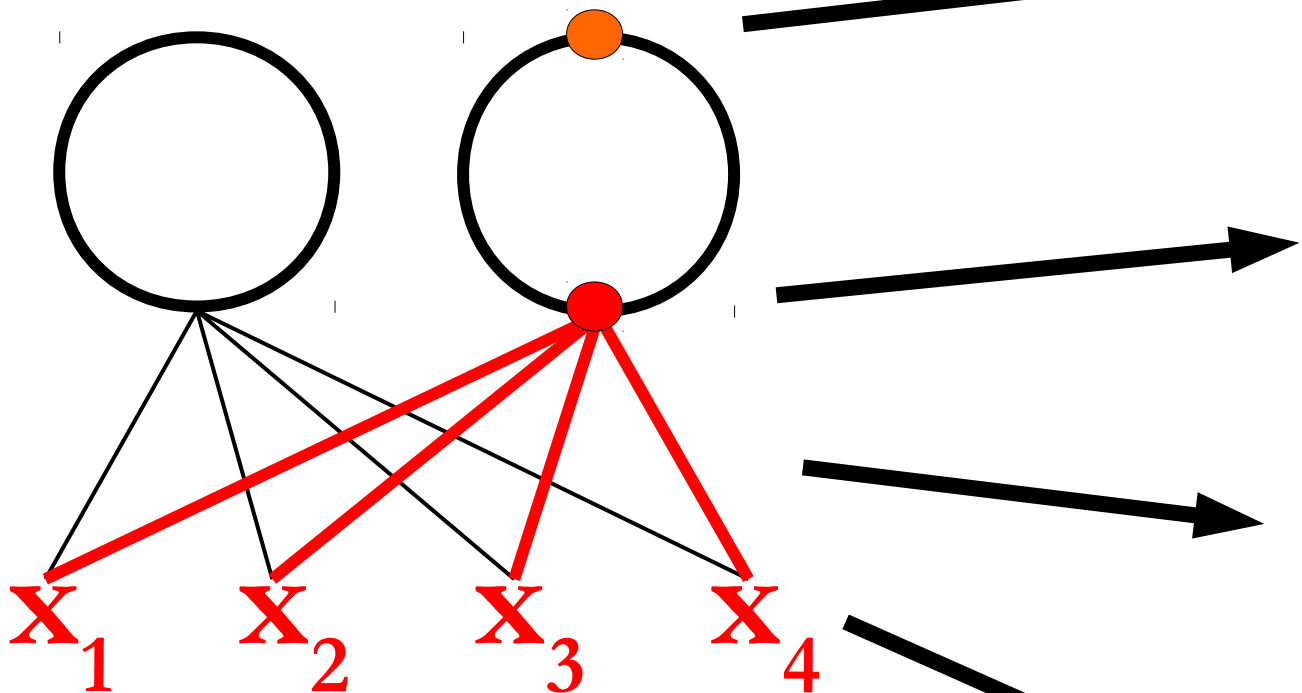


$$\begin{bmatrix} [1 & 0] \\ [1 & 1] \\ [0 & 1] \end{bmatrix}$$

$$\begin{bmatrix} [5.21 & -1.65] \\ [2.32 & 3.45] \\ [0.38 & 5.30] \end{bmatrix}$$

$$\begin{bmatrix} [0.9 & 0.8 & -1.0 & -1.0] \\ [-0.5 & -0.5 & 1.5 & 1.0] \end{bmatrix}$$

$$\begin{bmatrix} [4.9 & 3.0 & 1.4 & 0.2] \\ [6.4 & 3.2 & 4.5 & 1.5] \\ [5.8 & 2.7 & 5.1 & 1.9] \end{bmatrix}$$

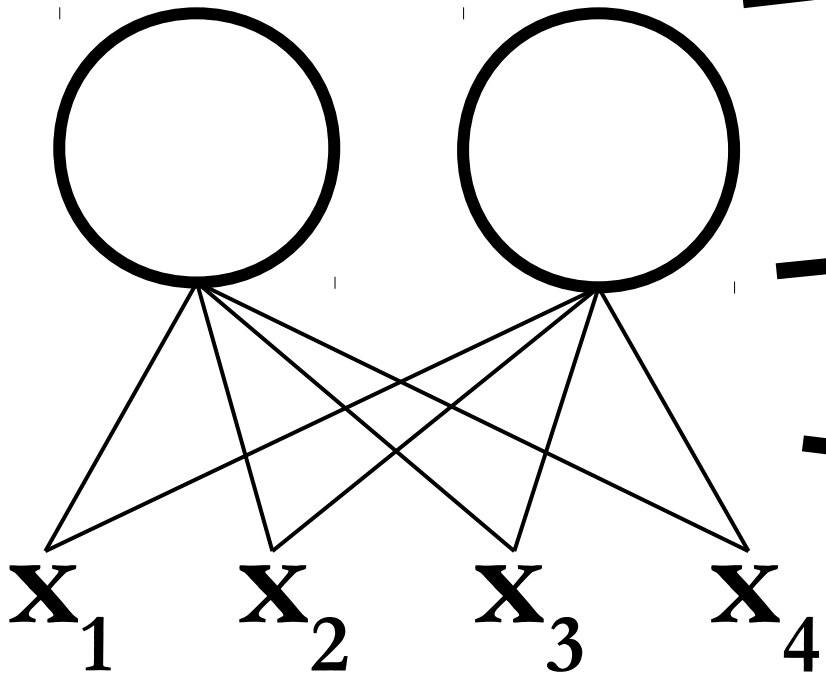


[[1 0]  
[1 1]  
[0 1]]

[[5.21 -1.65]  
[2.32 3.45]  
[0.38 5.30]]

[[ 0.9 0.8 -1.0 -1.0]  
[-0.5 -0.5 1.5 1.0]]

[[4.9 3.0 1.4 0.2]  
[6.4 3.2 4.5 1.5]  
[5.8 2.7 5.1 1.9]]



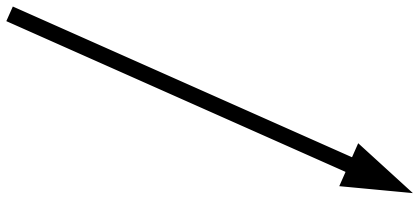
$$\begin{bmatrix} [1 & 0] \\ [1 & 1] \\ [0 & 1] \end{bmatrix}$$



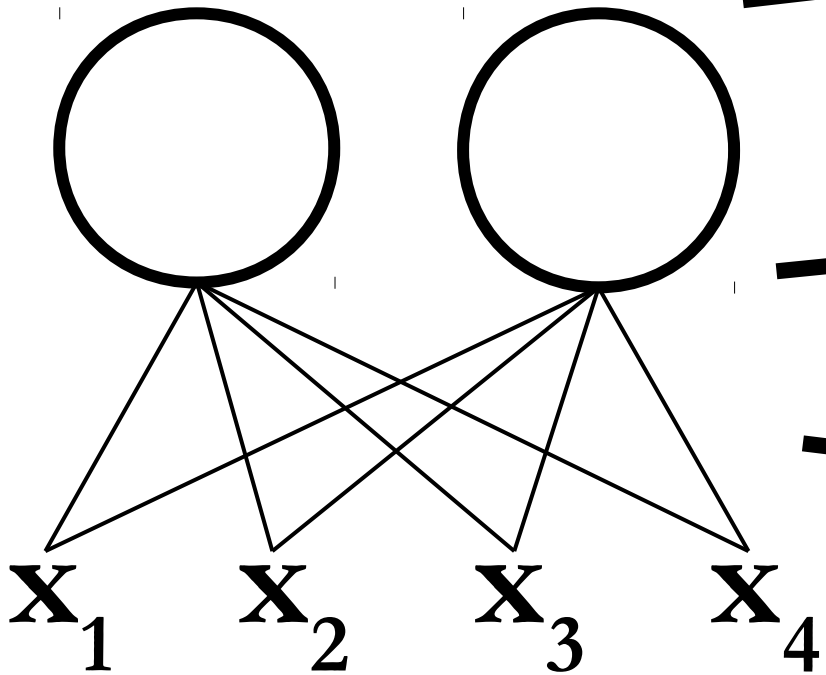
$$\begin{bmatrix} [5.21 & -1.65] \\ [2.32 & 3.45] \\ [0.38 & 5.30] \end{bmatrix}$$



$$\begin{bmatrix} [0.9 & 0.8 & -1.0 & -1.0] \\ [-0.5 & -0.5 & 1.5 & 1.0] \end{bmatrix}$$



$$\begin{bmatrix} [4.9 & 3.0 & 1.4 & 0.2] \\ [6.4 & 3.2 & 4.5 & 1.5] \\ [5.8 & 2.7 & 5.1 & 1.9] \end{bmatrix}$$



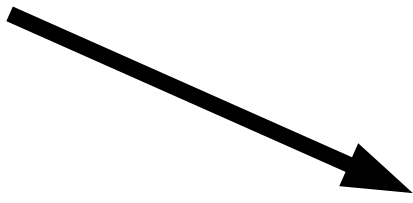
$$\begin{bmatrix} [1 & 0] \\ [1 & 1] \\ [0 & 1] \end{bmatrix}$$



$$\begin{bmatrix} [5.21 & -1.65] \\ [2.32 & 3.45] \\ [0.38 & 5.30] \end{bmatrix}$$

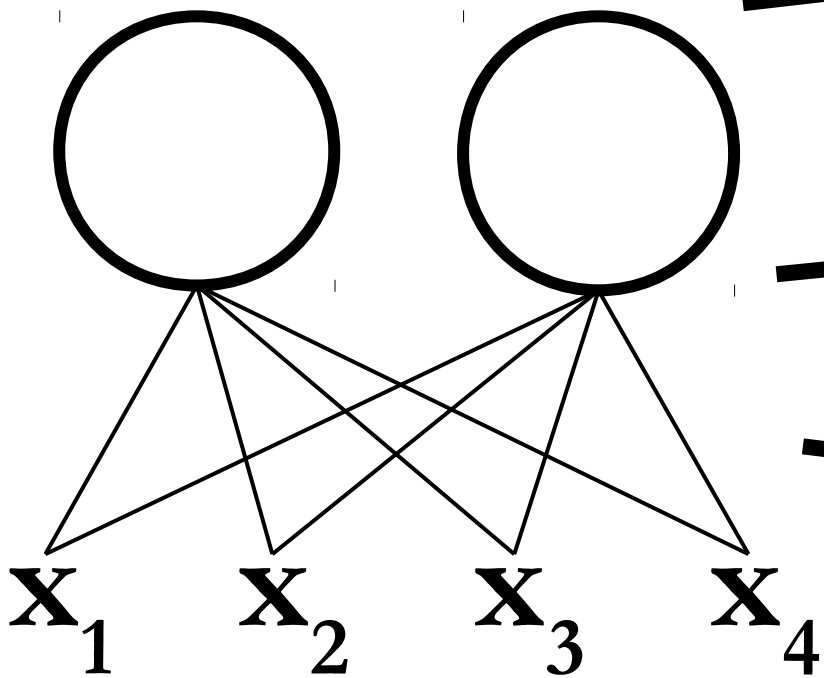


$$\begin{bmatrix} [0.9 & 0.8 & -1.0 & -1.0] \\ [-0.5 & -0.5 & 1.5 & 1.0] \end{bmatrix}$$



$$\begin{bmatrix} [4.9 & 3.0 & 1.4 & 0.2] \\ [6.4 & 3.2 & 4.5 & 1.5] \\ [5.8 & 2.7 & 5.1 & 1.9] \end{bmatrix}$$





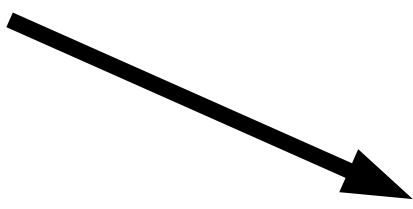
[[1 0]  
[1 1]  
**[0 1]**]



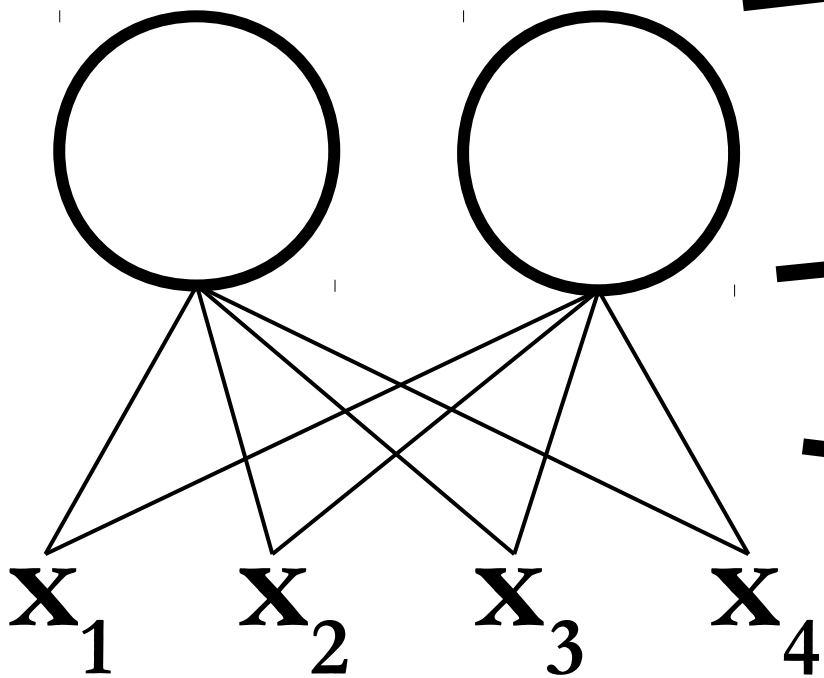
[[5.21 -1.65]  
[2.32 3.45]  
**[0.38 5.30]**]



**[[ 0.9 0.8 -1.0 -1.0]**  
[-0.5 -0.5 1.5 1.0]]



[[4.9 3.0 1.4 0.2]  
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**[5.8 2.7 5.1 1.9]**]



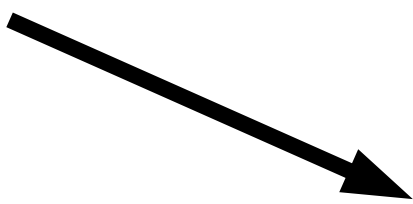
$$\begin{bmatrix} [1 & 0] \\ [1 & 1] \\ [0 & 1] \end{bmatrix}$$



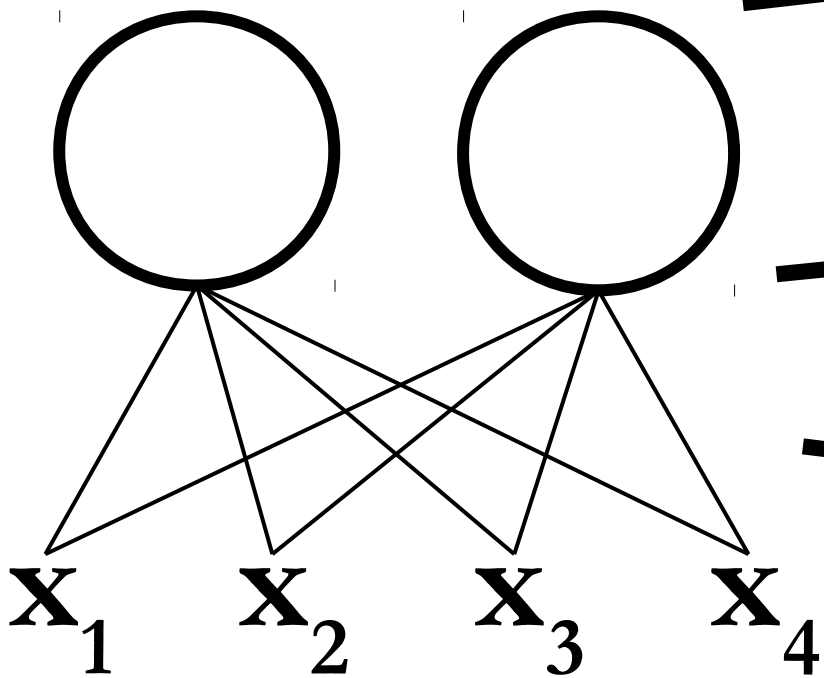
$$\begin{bmatrix} [5.21 & -1.65] \\ [2.32 & 3.45] \\ [0.38 & 5.30] \end{bmatrix}$$



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$$\begin{bmatrix} [4.9 & 3.0 & 1.4 & 0.2] \\ [6.4 & 3.2 & 4.5 & 1.5] \\ [5.8 & 2.7 & 5.1 & 1.9] \end{bmatrix}^{10}$$



$$\begin{bmatrix} [1 & 0] \\ [1 & 1] \\ [0 & 1] \end{bmatrix}$$

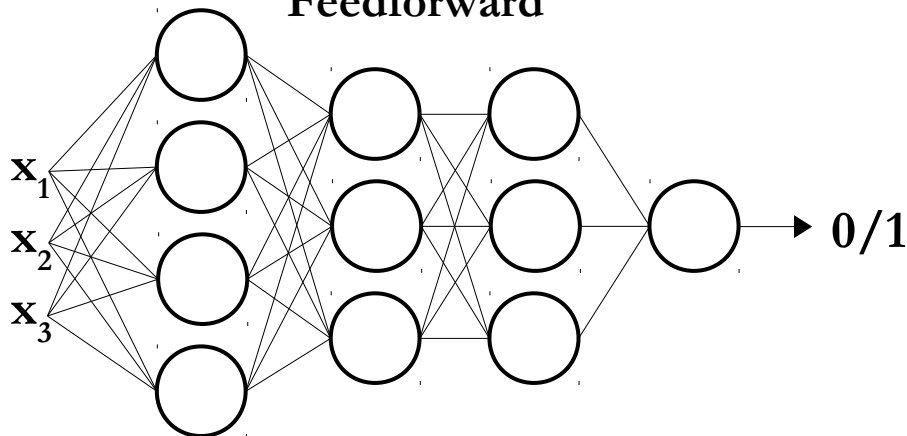
$$\begin{bmatrix} [5.21 & -1.65] \\ [2.32 & 3.45] \\ [0.38 & 5.30] \end{bmatrix}$$

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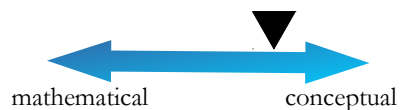
$$\begin{bmatrix} [4.9 & 3.0 & 1.4 & 0.2] \\ [6.4 & 3.2 & 4.5 & 1.5] \\ [5.8 & 2.7 & 5.1 & 1.9] \end{bmatrix}^{11}$$

# Deep Learning

Feedforward

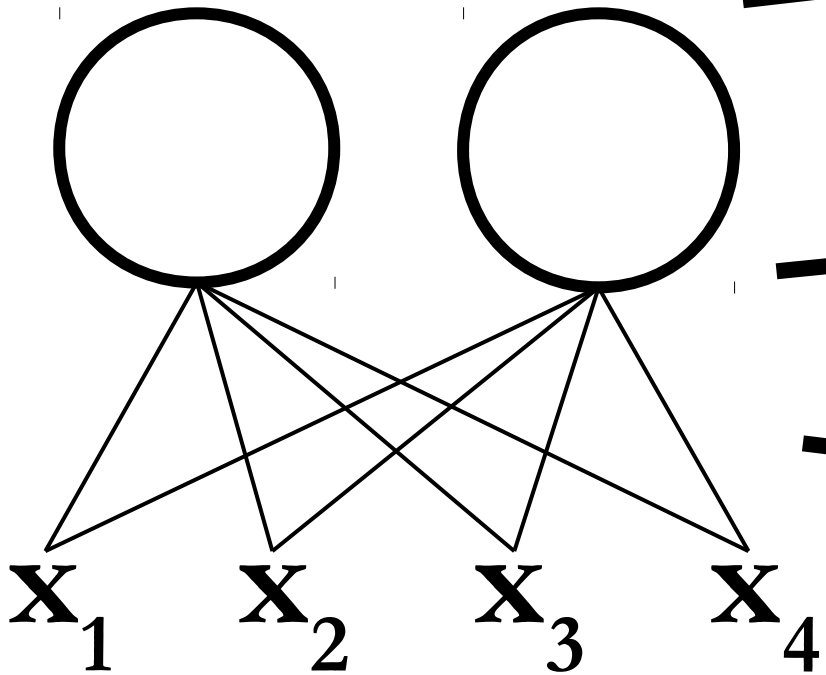


How does the algorithm make a decision?



How do you determine the right parameters for the algorithm?





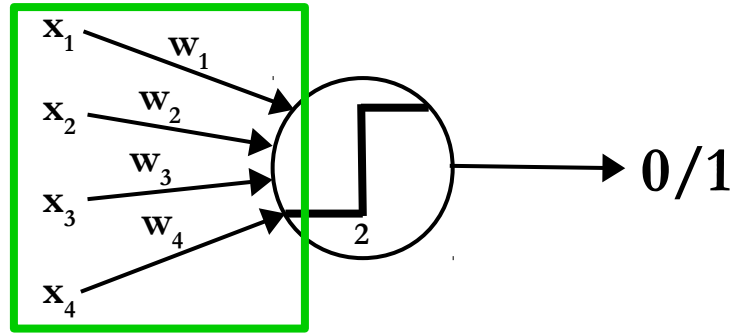
$$\begin{bmatrix} [1 & 0] \\ [1 & 1] \\ [0 & 1] \end{bmatrix}$$

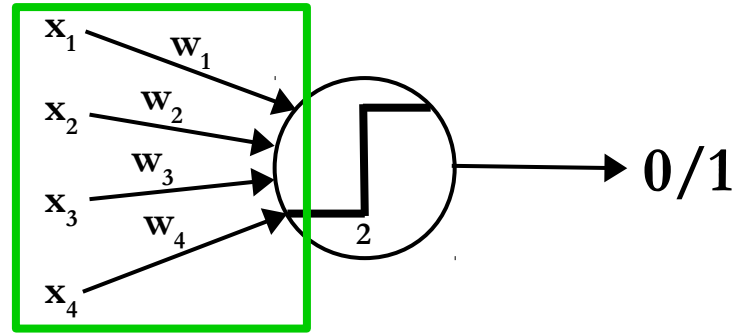
$$\begin{bmatrix} [[5.21 & -1.65] \\ [2.32 & 3.45] \\ [0.38 & 5.30]] \end{bmatrix}$$

$$\left\{ \begin{bmatrix} [0.9 & 0.8 & -1.0 & -1.0] \\ [-0.5 & -0.5 & 1.5 & 1.0] \end{bmatrix} \right.$$

$$\left\{ \begin{bmatrix} [4.9 & 3.0 & 1.4 & 0.2] \\ [6.4 & 3.2 & 4.5 & 1.5] \\ [5.8 & 2.7 & 5.1 & 1.9] \end{bmatrix} \right.$$

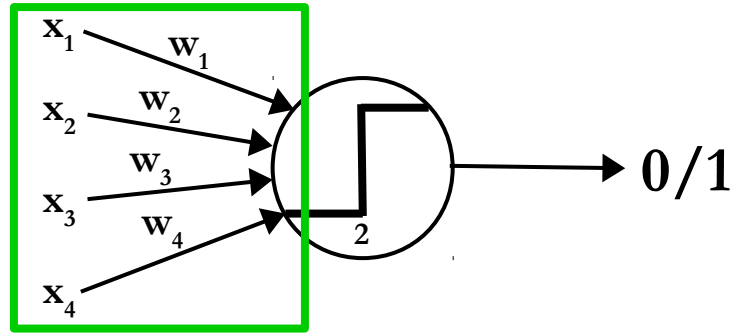
Number of examples \* number of nodes \* number of input values = number of iterations





## Weighted Sum

$$\sum_{i=1}^4 x_i w_i = x_1 w_1 + x_2 w_2 + x_3 w_3 + x_4 w_4$$



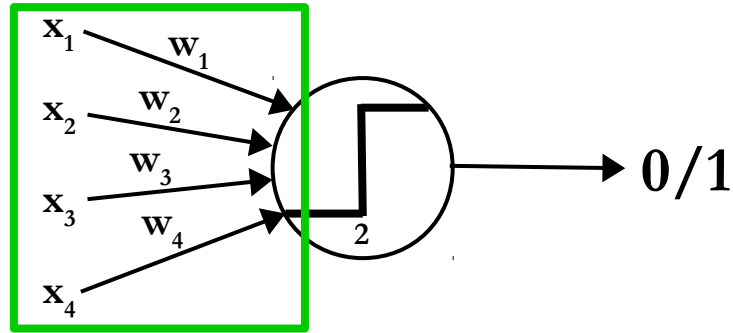
## Weighted Sum

$$\sum_{i=1}^4 x_i w_i = x_1 w_1 + x_2 w_2 + x_3 w_3 + x_4 w_4$$

## Dot Product

$$\vec{x} \cdot \vec{w} = x_1 w_1 + x_2 w_2 + x_3 w_3 + x_4 w_4$$





## Weighted Sum

$$\sum_{i=1}^4 x_i w_i = x_1 w_1 + x_2 w_2 + x_3 w_3 + x_4 w_4$$

## Dot Product

$$\begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix} \cdot \begin{pmatrix} w_1 \\ w_2 \\ w_3 \\ w_4 \end{pmatrix} = x_1 w_1 + x_2 w_2 + x_3 w_3 + x_4 w_4$$

# Linear Algebra

- BLAS, LAPACK → optimized algorithms

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- C, Fortran → low-level languages

# Linear Algebra

- BLAS, LAPACK → optimized algorithms
- C, Fortran → low-level languages
- SIMD → parallel processing

# Multiplying respective Elements of two Lists

```
list_1 = [1, 2, 5]  
list_2 = [4, 7, 3]
```



pure Python



SIMD

```
list_3 = []  
for value_1, value_2 in zip(list_1, list_2):  
    value_3 = value_1 * value_2  
    list_3.append(value_3)
```

```
print(list_3)
```

```
[4, 14, 15]
```

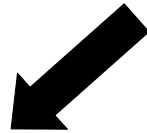
```
list_3 = list_1 * list_2
```

```
print(list_3)
```

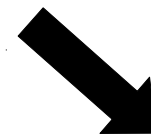
```
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pure Python



SIMD/Vectorization

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    value_3 = value_1 * value_2  
    list_3.append(value_3)
```

```
print(list_3)
```

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```
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```
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```

# Linear Algebra

- BLAS, LAPACK → optimized algorithms

- C, Fortran → low-level languages

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} NumPy